
Computer Graphics

7 - Mesh 2, Lighting & Shading 1

Yoonsang Lee
Spring 2022

Midterm Exam Announcement

- Date & time: **Apr 27**, 09:30 - 10:30 am
- Place: IT.BT, 508
- Scope: Lecture 2 ~ 7

- **You cannot leave the room until the end of the exam** even if you finish the exam earlier.

- Please bring your student ID card to the exam.

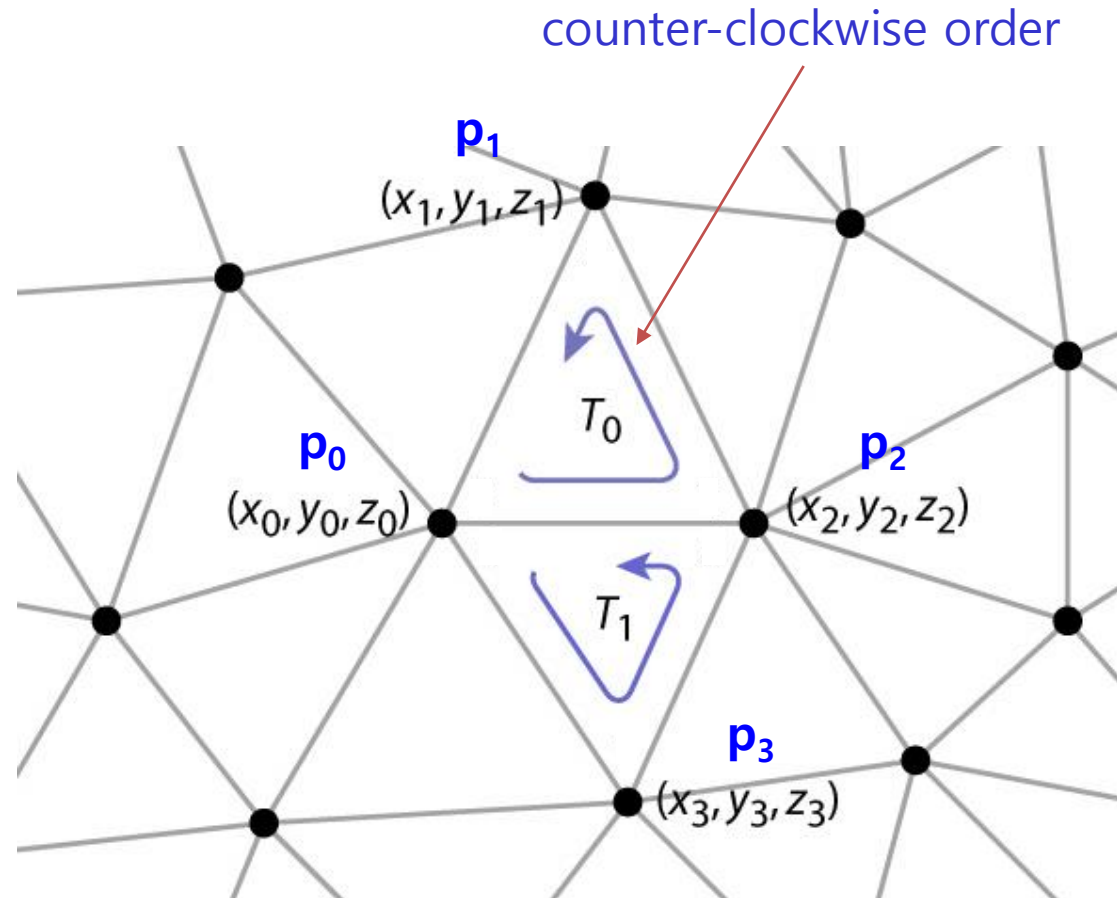
- If you are unable to take the offline exam (stay abroad, corona confirmed, etc.), please contact the TA in advance.
 - Chaejun Sohn (손채준 조교), thscowns@gmail.com
 - **You must inform the TA at least two days before the exam.**

Topics Covered

- Mesh
 - Representations for triangle meshes - Indexed triangle set
 - OBJ file format
- Reflection of Light
- Phong Illumination Model
- Shading
 - Face / Vertex Normal
 - Flat / Goraud / Phong Shading

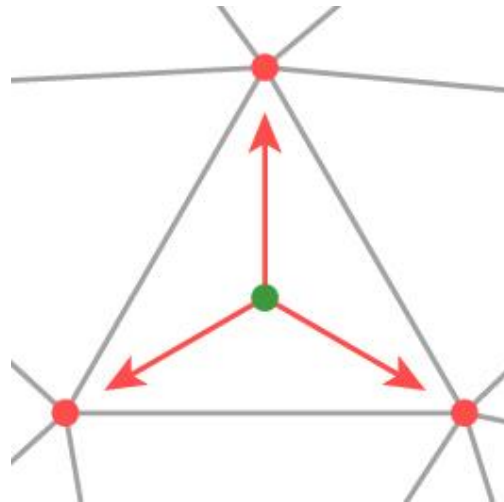
Recall: Separate triangles

	[0]	[1]	[2]
tris[0]	x_0, y_0, z_0	x_2, y_2, z_2	x_1, y_1, z_1
tris[1]	x_0, y_0, z_0	x_3, y_3, z_3	x_2, y_2, z_2
	⋮	⋮	⋮



Indexed triangle set

- Store each vertex once
- Each triangle points to its three vertices



Indexed triangle set

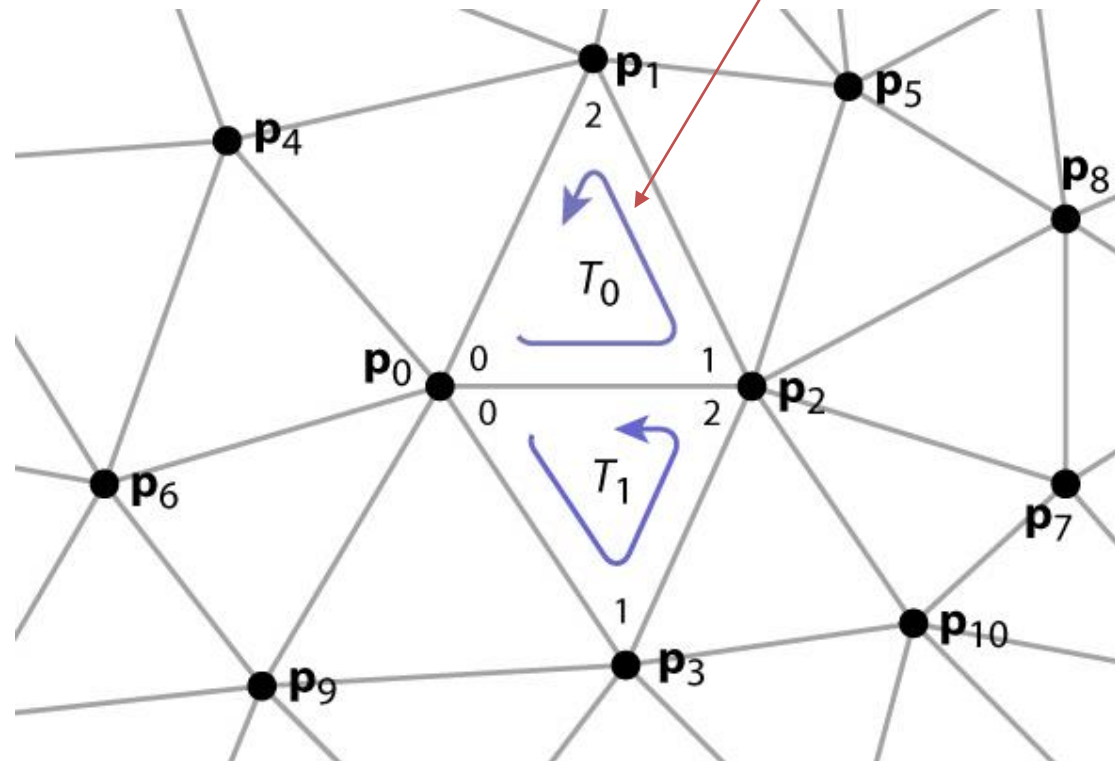
counter-clockwise order

vertex array

verts[0]	x_0, y_0, z_0
verts[1]	x_1, y_1, z_1
	x_2, y_2, z_2
	x_3, y_3, z_3
	\vdots

index array

tInd[0]	0, 2, 1
tInd[1]	0, 3, 2
	\vdots



Indexed Triangle Set

- Memory efficient: each vertex position is stored only once.
- Represents topology and geometry separately.
- Finding neighbor triangles is at least well defined.
 - Neighbor triangles share same vertex indices.

Drawing Indexed Triangles using Vertex & Index Array

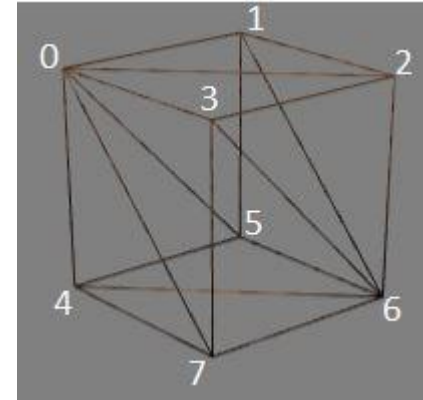
- 1. Create a vertex array & **index array** for your mesh
 - The vertex array **should not have duplicate vertex data**
- 2. Specify “pointer” to this vertex array
 - Same with the separate triangles case
- 3. Render the mesh using the specified “pointer” & the pointer to the **index array** (which contains vertex indices to be rendered)
 - Using **glDrawElements()**

glDrawElements()

- **glDrawElements(mode , count , type , indices)**
- : render primitives from vertex & index array data
 - **mode**: The primitive type to render. GL_POINTS, GL_TRIANGLES, ...
 - **count**: The number of vertex indices to be rendered
 - **type**: The type of the values in **indices**.
GL_UNSIGNED_BYTE, GL_UNSIGNED_SHORT, or
GL_UNSIGNED_INT
 - **indices**: The pointer to the index array

[Practice] Drawing Indexed Triangles using Vertex & Index Array

```
def createVertexAndIndexArrayIndexed():  
    varr = np.array([  
        (-1, 1, 1), # v0  
        (1, 1, 1), # v1  
        (1, -1, 1), # v2  
        (-1, -1, 1), # v3  
        (-1, 1, -1), # v4  
        (1, 1, -1), # v5  
        (1, -1, -1), # v6  
        (-1, -1, -1), # v7  
    ], 'float32')  
    iarr = np.array([  
        (0, 2, 1),  
        (0, 3, 2),  
        (4, 5, 6),  
        (4, 6, 7),  
        (0, 1, 5),  
        (0, 5, 4),  
        (3, 6, 2),  
        (3, 7, 6),  
        (1, 2, 6),  
        (1, 6, 5),  
        (0, 7, 3),  
        (0, 4, 7),  
    ],  
    )  
    return varr, iarr
```



vertex index	position
0	(-1, 1, 1)
1	(1, 1, 1)
2	(1, -1, 1)
3	(-1, -1, 1)
4	(-1, 1, -1)
5	(1, 1, -1)
6	(1, -1, -1)
7	(-1, -1, -1)

Starts from the "[Practice] Drawing Separate Triangles using Vertex Array" code in the prev. lecture,

```
def render():
    # ...
    drawFrame()
    glColor3ub(255, 255, 255)
    drawCube_glDrawElements()

def drawCube_glDrawElements():
    global gVertexArrayIndexed, gIndexArray
    varr = gVertexArrayIndexed
    iarr = gIndexArray
    glEnableClientState(GL_VERTEX_ARRAY)
    glVertexPointer(3, GL_FLOAT, 3*varr.itemsize, varr)
    glDrawElements(GL_TRIANGLES, iarr.size, GL_UNSIGNED_INT, iarr)

# ...
gVertexArrayIndexed = None
gIndexArray = None

def main():
    # ...
    global gVertexArrayIndexed, gIndexArray

    # ...
    gVertexArrayIndexed, gIndexArray = createVertexAndIndexArrayIndexed()

    while not glfw.window_should_close(window):
        # ...
```

Quiz #1

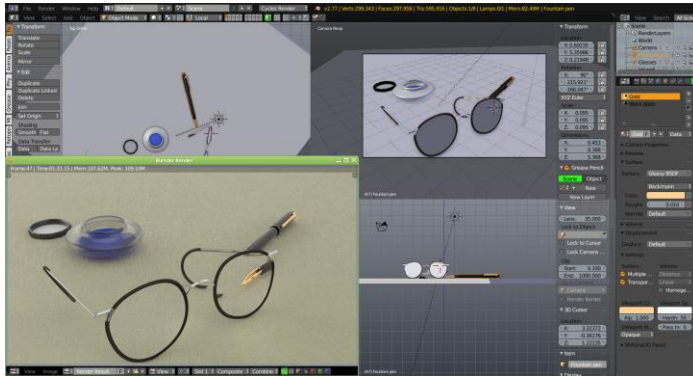
- Go to <https://www.slido.com/>
- Join #cg-ys
- Click “Polls”

- Submit your answer in the following format:
 - **Student ID: Your answer**
 - e.g. **2017123456: 4)**

- Note that you must submit all quiz answers in the above format to be checked for “attendance”.

Do we need to hard-code all vertex positions and indices?

- Of course not!
- An *object file* or *model file* storing polygon mesh data is usually created using 3D modeling tools.



Blender



Maya

- Applications (such as games) usually load vertex and index data from an *object file* and draw the object using the loaded data.

3D Model File Formats

- DXF – AutoCAD
 - Supports 2-D and 3-D; binary
- 3DS – 3DS MAX
 - Flexible; binary
- VRML – Virtual reality modeling language
 - ASCII – Human readable (and writeable)
- **OBJ – Wavefront OBJ format**
 - ASCII – Human readable (and writeable)
 - Extremely simple
 - Widely supported
- Let's take a closer look at OBJ format!

OBJ File Format

```
# this is a comment

# List of vertex positions, in (x, y, z) form.
v 0.123 0.234 0.345
v 0.2 0.5 0.3
v ...
...

# List of vertex normals, in (x,y,z) form; normals
might not be unit vectors.
vn 0.707 0.000 0.707
vn ...
...

# List of vertex texture coordinates, in (u, v) form.
vt 0.500 1
vt ...
...
```

OBJ File Format

```
# List of faces (all argument indices are 1-based indices!)

# with vertex positions only - vertex_position_index
f 1 2 3
f 2 3 4
...

#
vertex_position_index/texture_coordinates_index/vertex_normal_index
f 6/4/1 3/5/3 7/6/5

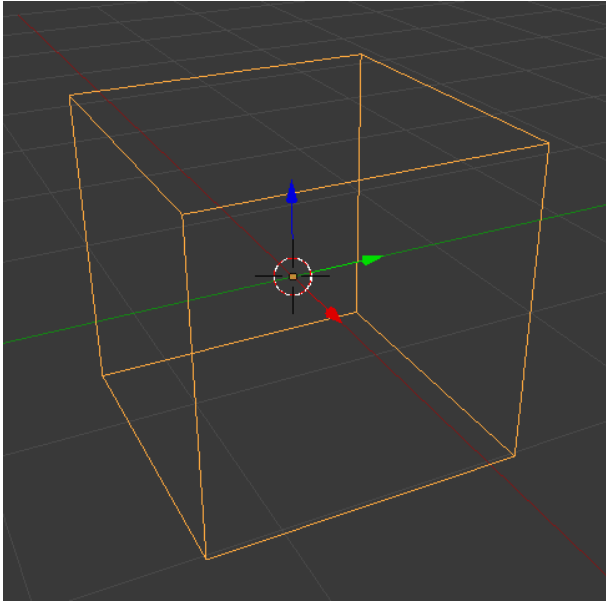
# vertex_position_index//vertex_normal_index
f 7//1 8//2 9//3
...

# vertex_position_index/texture_coordinates_index
f 3/1 4/2 5/3
...
```


OBJ File Format

- Other supported features:
 - for parameter space vertices for free from geometry
 - `vp 0.310000 3.210000 2.100000`
 - for polyline
 - `1 5 8 1 2 4 9`
 - for reference materials
 - `mtllib [external .mtl file name]`
 - `usemtl [material name]`
 - ...
- You don't need to use these features in this class.

An OBJ Example



```
# A simple cube
v 1.000000 -1.000000 -1.000000
v 1.000000 -1.000000 1.000000
v -1.000000 -1.000000 1.000000
v -1.000000 -1.000000 -1.000000
v 1.000000 1.000000 -1.000000
v 1.000000 1.000000 1.000000
v -1.000000 1.000000 1.000000
v -1.000000 1.000000 -1.000000
f 1 2 3 4
f 5 8 7 6
f 1 5 6 2
f 2 6 7 3
f 3 7 8 4
f 5 1 4 8
```

[Practice] Manipulate an OBJ file with Blender

- Blender
 - <https://www.blender.org/>
 - Open source
 - Full 3D modeling/rendering/animation tool
- Install & launch Blender
- Reference for basic mouse actions in Blender
 - https://en.wikibooks.org/wiki/Blender_3D:_Noob_to_Pro/3D_View_Windows#Changing_Your_Viewpoint,_Part_One

[Practice] Manipulate an OBJ file with Blender

- Save the obj example in the prev. page as cube.obj (using a text editor)
- Click the "start-up" cube object in the Blender and press Del key to delete it.
- Import cube.obj into Blender (File-Import)
 - Press 'z' to render in wireframe mode
- Edit cube.obj somehow (using a text editor)
- Delete the loaded cube and re-import cube.obj into Blender again
- Press 'tab' to switch to *Edit mode*

[Practice] Manipulate an OBJ file with Blender

- Click to select a vertex and click "move" icon from the left icons (or press 'G')
- Move the selected vertex by dragging red/blue/green arrows
- Export this mesh to cube.obj (File – Export)
- Open cube.obj using a text editor and check what is changed
- Reference for *Edit mode* in Blender
 - https://en.wikibooks.org/wiki/Blender_3D:_Noob_to_Pro/Mesh_Edit_Mode
- Reference for *Object mode* in Blender
 - https://en.wikibooks.org/wiki/Blender_3D:_Noob_to_Pro/Object_Mode

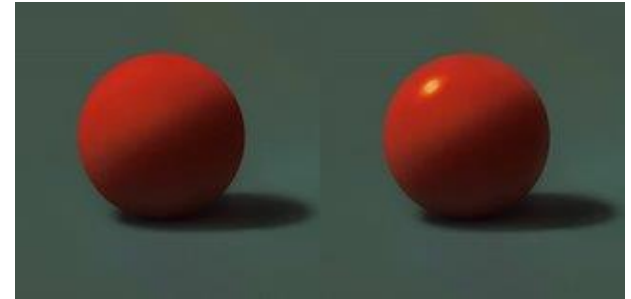
OBJ Sources

- <https://free3d.com/>
- <https://www.cgtrader.com/free-3d-models>
- You can download any .obj model files from these sites and open them in Blender.
- OBJ file format is very popular:
 - Most modeling programs will export OBJ files
 - Most rendering packages will read in OBJ files

Reflection of Light

Reflection of Light

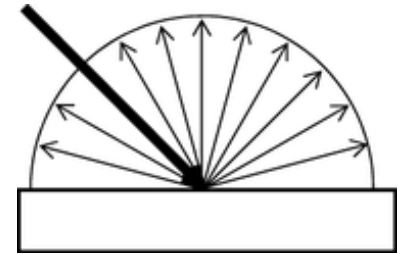
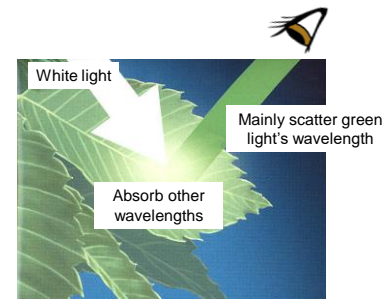
- Light can be absorbed(흡수), emitted(발산), scattered(산란), reflected(반사), or refracted(굴절) by objects.
- Scattering and reflection are the main factors in the visual characteristics of a object surface.
 - such as surface color, highlight on surface
- Types of reflection:
 - Diffuse reflection
 - Specular reflection
 - Ideal specular reflection
 - Non-ideal specular reflection (a.k.a. Glossy reflection)



* In computer graphics, both scattering and reflection are often referred to as "reflection"

Diffuse Reflection

- : Scattering specific light spectrum in all direction
- → Determines surface color
- **View-independent**



strongly scatters
magenta's wavelengths



scatter all wavelengths with
roughly equal strength



absorb all wavelengths
(scatters little)

Diffuse Reflection - Lambert's Cosine Law

- The **reflected energy** from a small surface area is proportional to the **cosine of the angle** between **incident light direction** and the **surface normal**

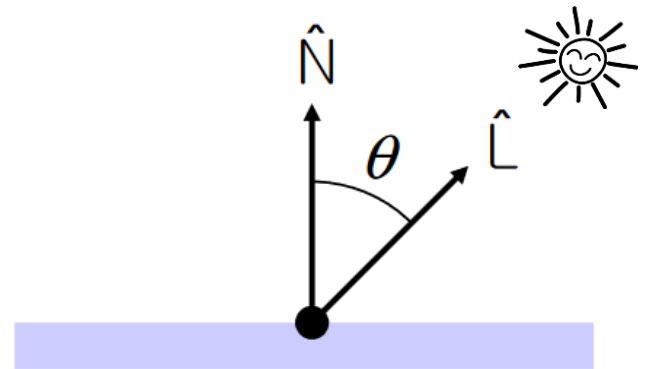
$$\begin{aligned} I_{reflected} &= I_{incident} \cos\theta \\ &= I_{incident} (\hat{\mathbf{N}} \cdot \hat{\mathbf{L}}) \end{aligned}$$

$I_{reflected}$ intensity of reflected ray

$I_{incident}$ intensity of incident ray

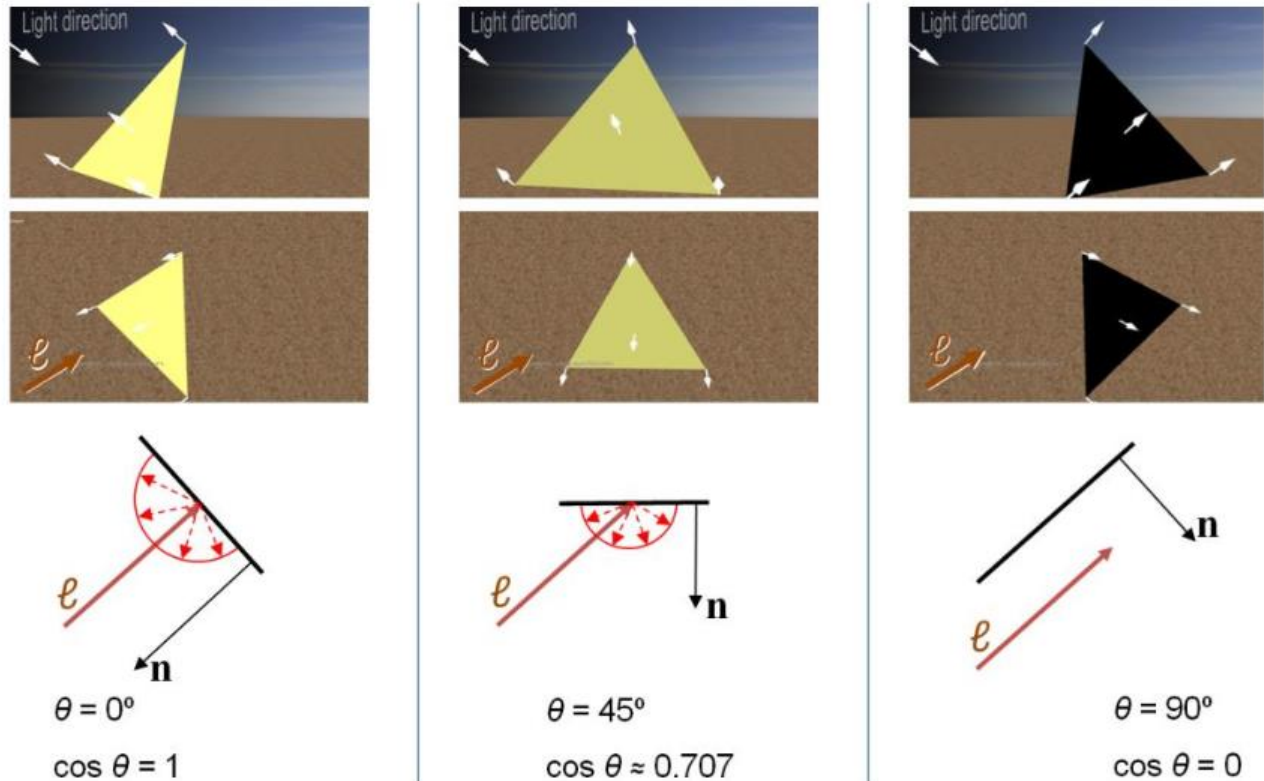
$\hat{\mathbf{N}}$ normal to the reflection surface at the point of the incidence

$\hat{\mathbf{L}}$ normalized light direction vector



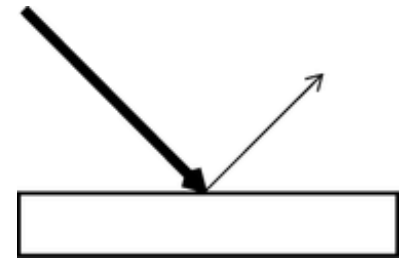
Diffuse Reflection - Lambert's Cosine Law

▶ Visualization of Lambert's law in 2D



Ideal Specular Reflection

- : Mirror-like reflection of light from smooth, polished surface
- → Generate mirrored images
- **View-dependent**



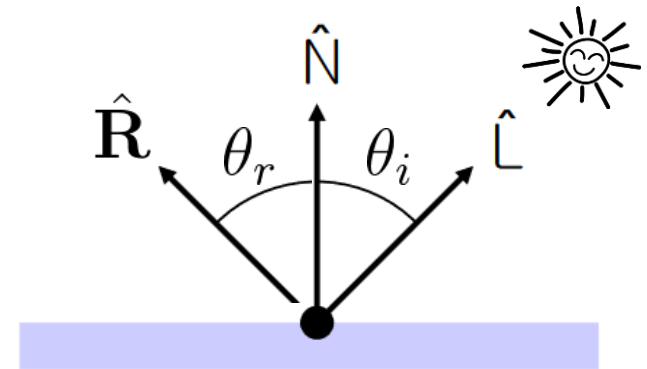
Ideal Specular Reflection - Laws of Reflection

- $\hat{\mathbf{N}}, \hat{\mathbf{L}}, \hat{\mathbf{R}}$ lie in the same plane
- $\theta_r = \theta_i$
- ($\hat{\mathbf{L}}$ and $\hat{\mathbf{R}}$ are on the opposite sides of $\hat{\mathbf{N}}$)

$\hat{\mathbf{N}}$ normal to the reflection surface at the point of the incidence

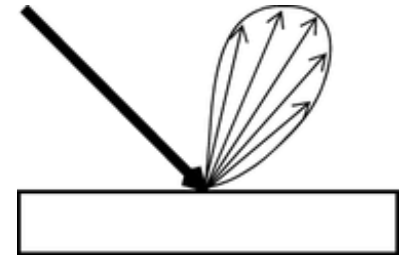
$\hat{\mathbf{L}}$ normalized incident ray direction vector

$\hat{\mathbf{R}}$ normalized reflected ray direction vector



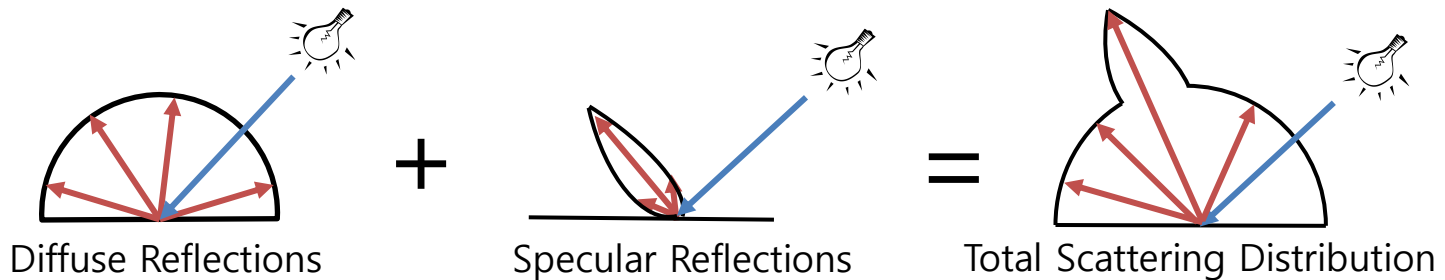
Non-Ideal Specular Reflection (a.k.a. Glossy Reflection)

- : Reflection on shiny & glossy surface, but not as smooth as a mirror
- Reflected rays are “spread out” due to surface roughness
- → Generate bright highlights
- **View-dependent**



Reflection of General Materials

- Many materials' surface have both diffuse reflection and (non-ideal) specular reflection.



Quiz #2

- Go to <https://www.slido.com/>
- Join #cg-ys
- Click “Polls”

- Submit your answer in the following format:
 - **Student ID: Your answer**
 - e.g. **2017123456: 4)**

- Note that you must submit all quiz answers in the above format to be checked for “attendance”.

Phong Illumination Model

Lighting (or Illumination)

- In computer graphics, **lighting** (or **illumination**) refers to the process of computing the effects of lights.
- → Computing surface color and highlights of objects.

Phong Illumination Model

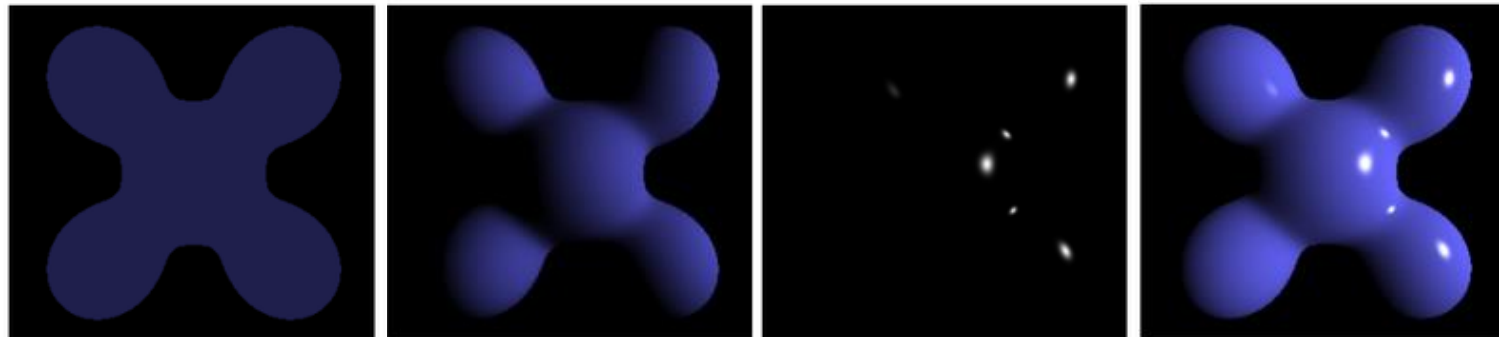
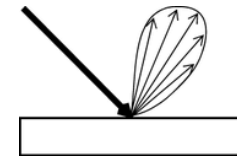
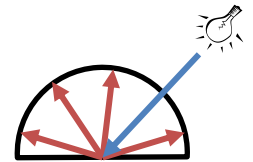
- One of the most commonly used “classical” illumination models in computer graphics
 - Empirical model, not physically based



Bùi Tường Phong
(1942 – 1975)

Phong Illumination Model

- Three components:
- **Ambient**
 - Non-specific constant global lighting
 - Crudest approximation for indirect lighting
- **Diffuse**
 - Color of object under normal conditions using Lambert's model
- **Specular**
 - Highlights on shiny objects
 - Approximation for glossy reflection using $\cos^n(\alpha)$



Ambient

+

Diffuse

+

Specular

=

Phong Reflection

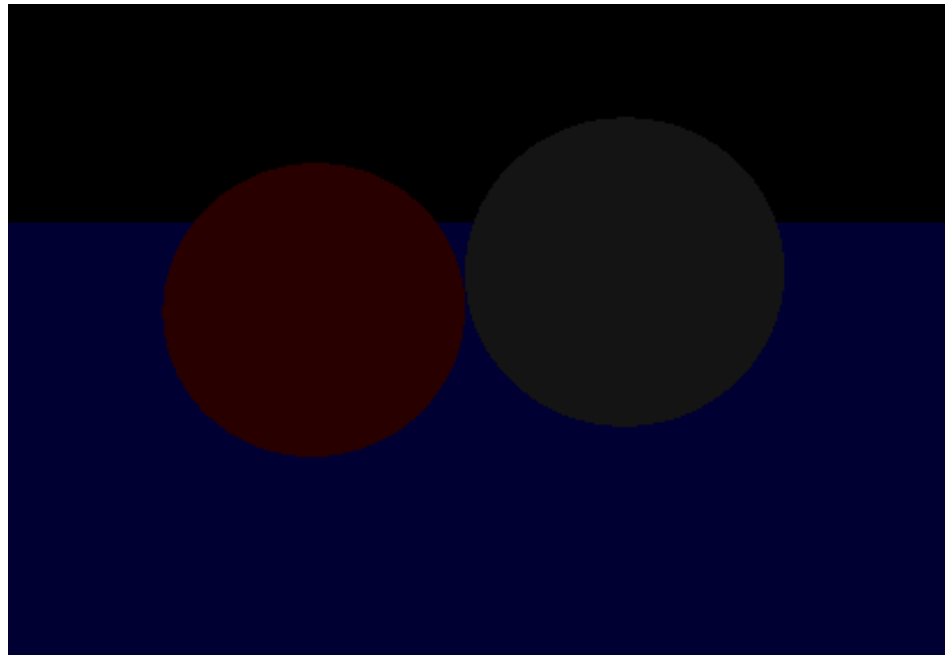
Ambient Light

$$I = k_a C_a$$

- C_a = intensity of ambient light
- k_a = ambient reflection coefficient
- Actually 3 equations for 3 C_a s! (C_a^r , C_a^g , C_a^b for Red, Green, Blue)
 - **Intensity I is calculated for any point on the surface of the object.**
 - for a polygon vertex
 - or for any interior point in a polygon (corresponds to a pixel in the film space).

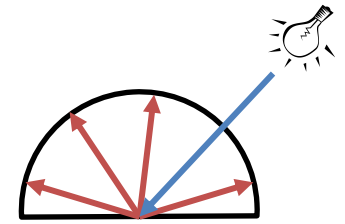
Total Illumination

$$I = k_a C_a$$



Diffuse Light

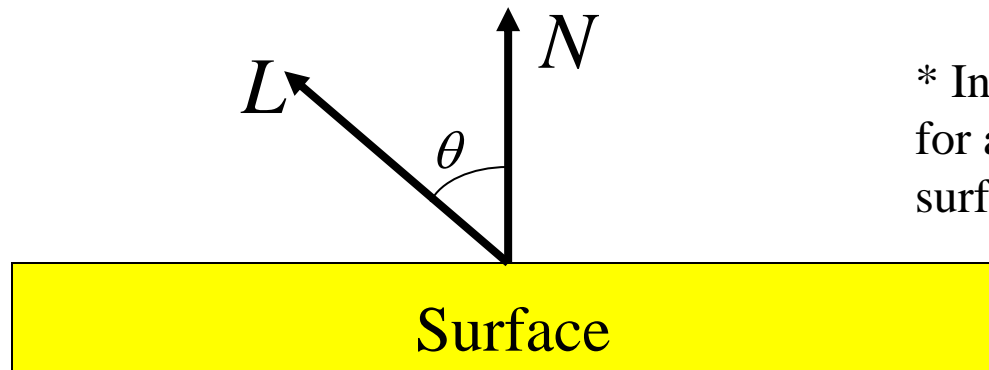
Lambert's Cosine Law



$$I = C_d k_d \cos(\theta) = C_d k_d (L \cdot N)$$

- C_d = intensity of diffuse light (actually 3 equations for C_d^r, C_d^g, C_d^b)
- k_d = diffuse reflection coefficient
- θ = angle between normal and direction to light

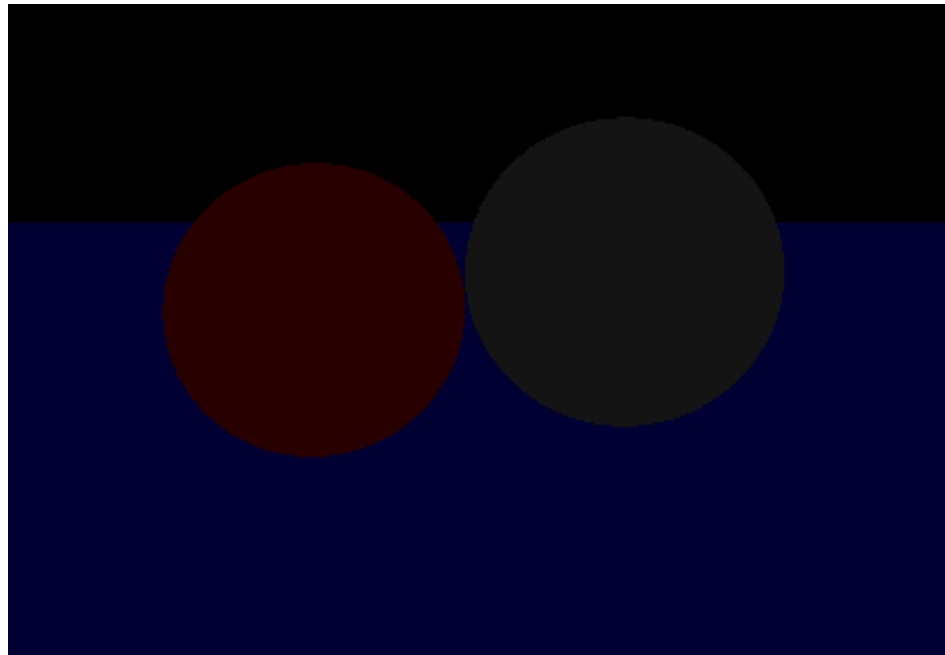
$$\cos(\theta) = L \cdot N$$



* Intensity I is calculated for any point on the surface of the object.

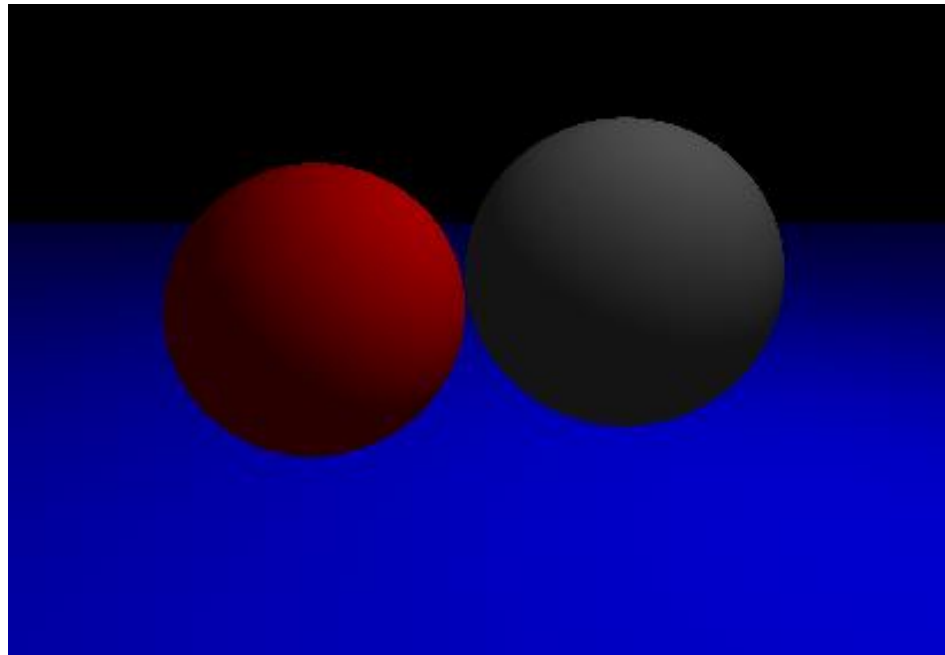
Total Illumination

$$I = k_a C_a$$



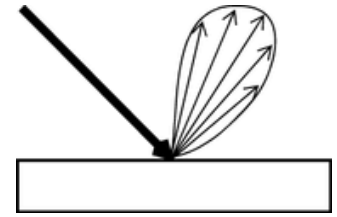
Total Illumination

$$I = k_a C_a + k_d C_d (L \cdot N)$$



Specular Light

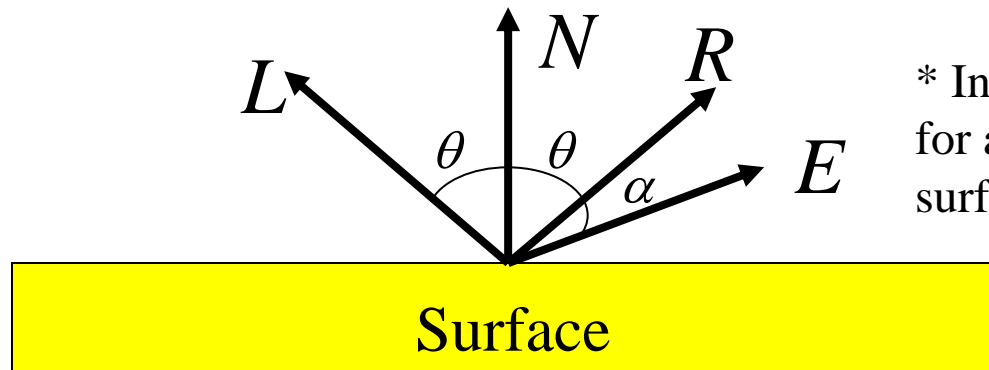
approximation for
glossy reflection



$$I = C_s k_s \cos^n(\alpha) = C_s k_s (R \cdot E)^n$$

- C_s = intensity of specular light (actually 3 eq: C_s^r, C_s^g, C_s^b)
- k_s = specular reflection coefficient
- α = angle between reflected vector (R) and eye (E)
- n = shininess coefficient

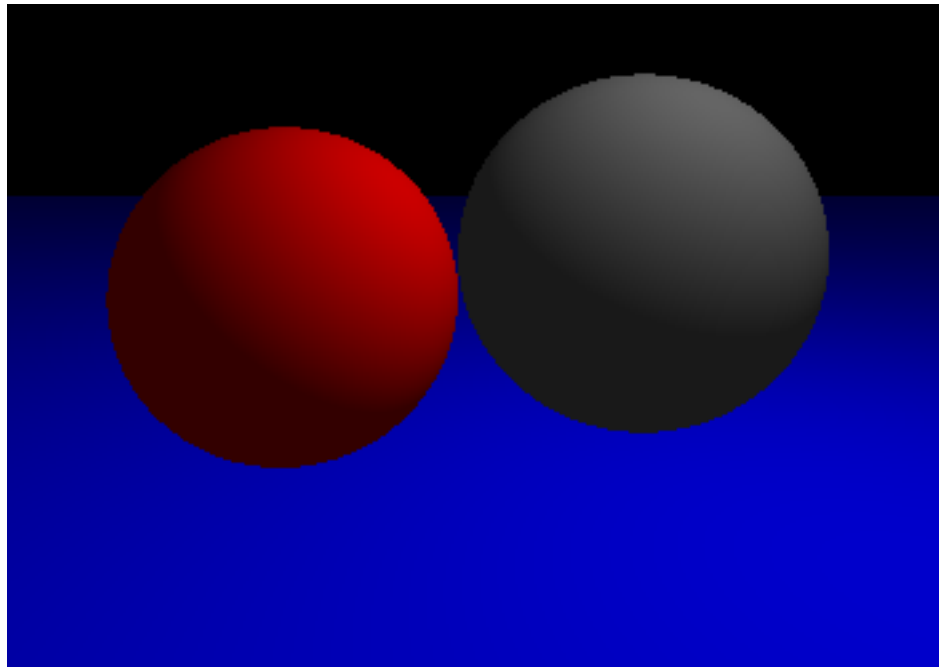
$$\cos(\alpha) = R \cdot E$$



* Intensity I is calculated for any point on the surface of the object.

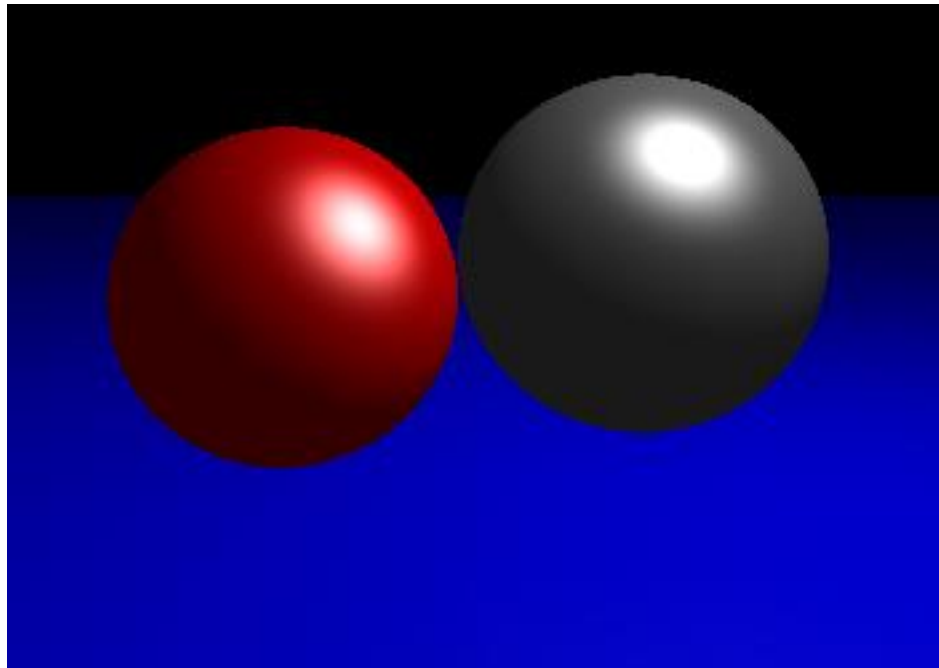
Total Illumination

$$I = k_a C_a + k_d C_d (L \cdot N)$$



Total Illumination

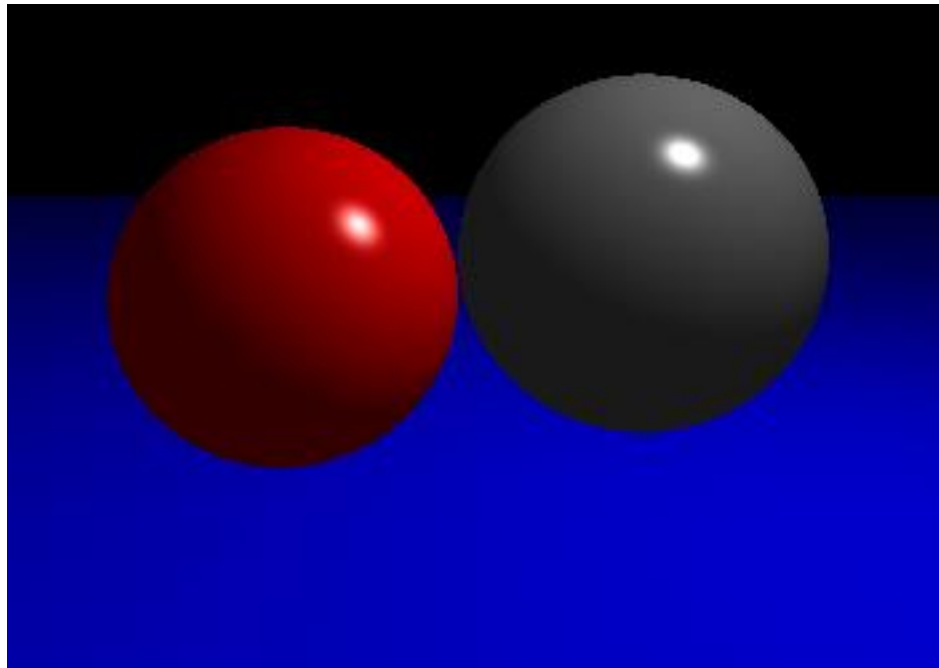
$$I = k_a C_a + k_d C_d (L \cdot N) + k_s C_s (R \cdot E)^n$$



$$n=5$$

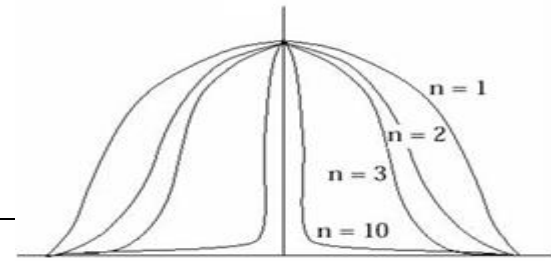
Total Illumination

$$I = k_a C_a + k_d C_d (L \cdot N) + k_s C_s (R \cdot E)^n$$



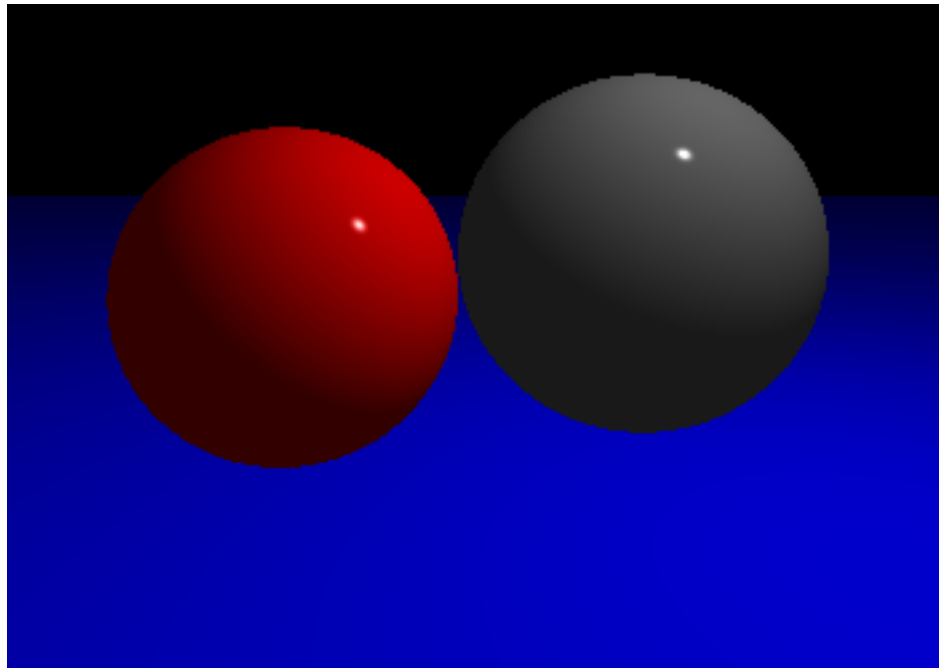
$n=50$

Total Illumination



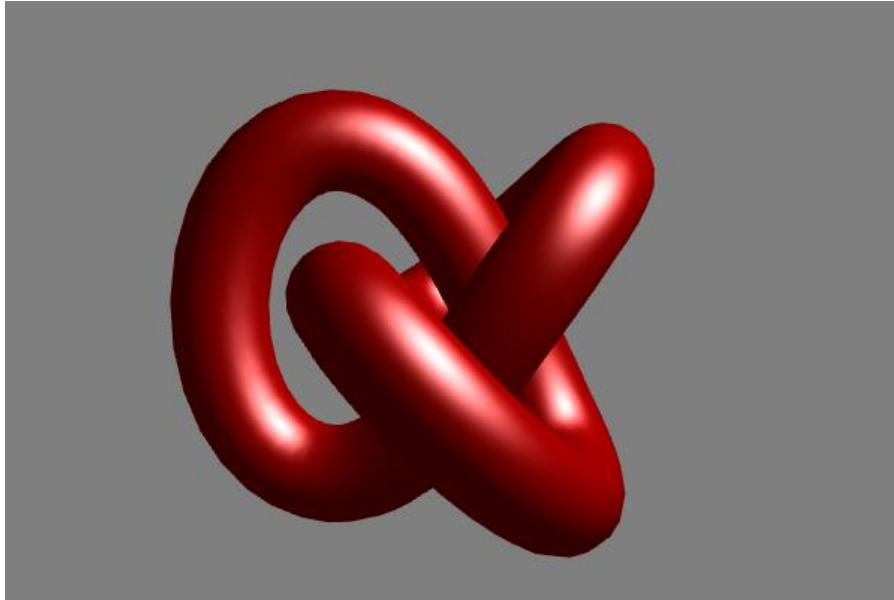
Specular falloff of $(\cos \delta)^n$

$$I = k_a C_a + k_d C_d (L \cdot N) + k_s C_s (R \cdot E)^n$$



$n = 500$

[Practice] Phong Illumination Demo



<http://www.cs.toronto.edu/~jacobson/phong-demo/>

- First set the value of the first drop down box to “Phong Shading”
- Try to change
 - reflection coefficient and color of ambient, diffuse, and specular
 - specular shininess
 - you can also change object type, light position and background color

Quiz #3

- Go to <https://www.slido.com/>
- Join #cg-ys
- Click “Polls”

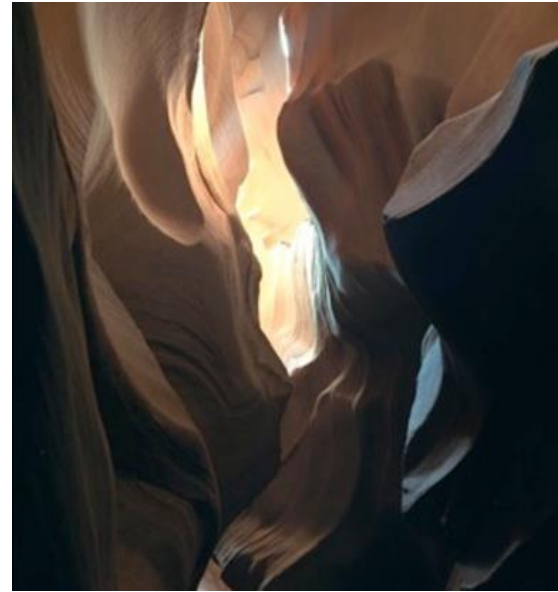
- Submit your answer in the following format:
 - **Student ID: Your answer**
 - e.g. **2017123456: 4)**

- Note that you must submit all quiz answers in the above format to be checked for “attendance”.

Shading

Shading - General Meaning

- Variation in observed color across an object
 - Strongly affected by lighting



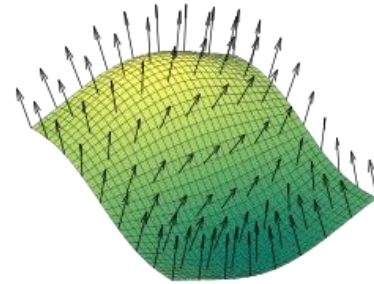
Shading - Meaning in Computer Graphics

- The process of determining **each pixel color in a polygon** based on a illumination model



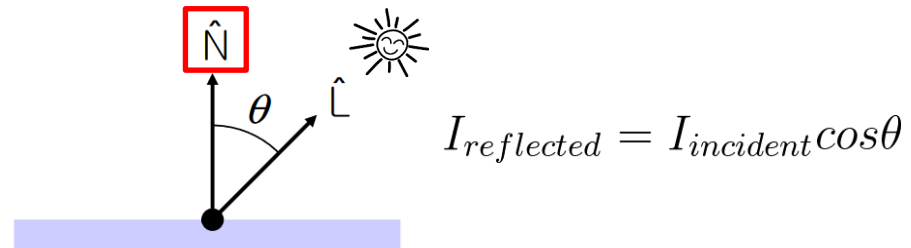
Surface Normal

- A vector that is perpendicular to the surface at a given point
 - A unit normal vector (of length 1) is generally used

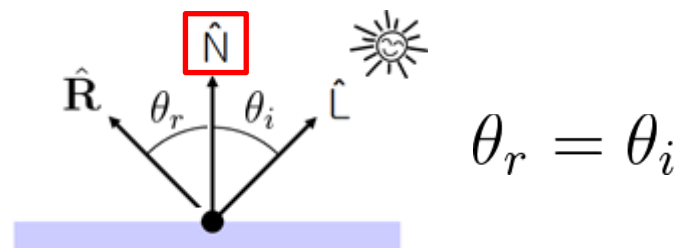


- Plays a key role in shading & illumination process

- Diffuse reflection
 - Lambert's Cosine Law



- Specular reflection
 - Laws of Reflection

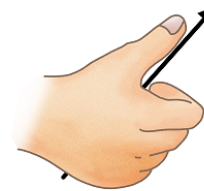
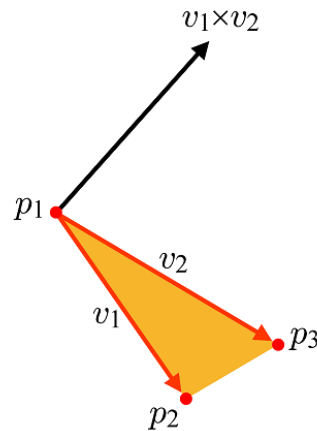
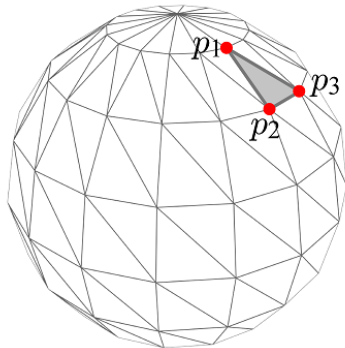


Face Normal

- How to get the surface normal of a polygonal face

The order does matter!

- The normal of a triangle $\langle p_1, p_2, p_3 \rangle$ is computed as $v_1 \times v_2$
 - v_1 is the vector connecting p_1 and p_2 , v_2 connects p_1 and p_3

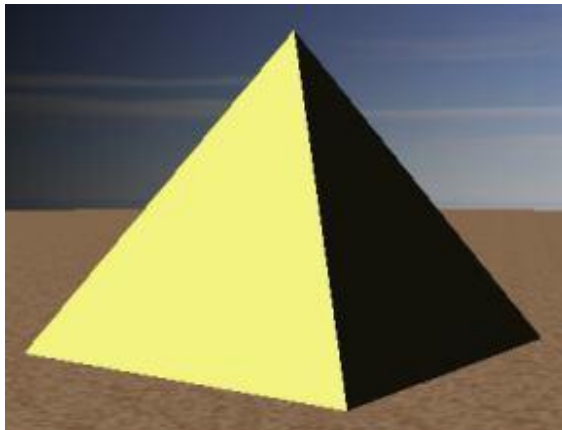


$$\frac{v_1 \times v_2}{\|v_1 \times v_2\|}$$

- That's why we need **counterclockwise** vertex ordering
 - The direction of a face normal determines “outside” of the face

Flat Shading

- Use a single face normal for each polygon
- Calculate color (by illumination) once per polygon
 - Typically use center of polygon
- Fast, but not very desirable for curved shapes
 - Even if we increase the number of polygons, it's still “faceted“

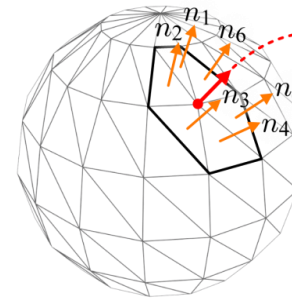


Smooth Shading

- Shading methods for curved shapes
 - Smooth color transition between two adjacent polygons



- Two methods:
 - Gouraud shading
 - Phong shading



$$\frac{n_1+n_2+n_3+n_4+n_5+n_6}{\|n_1+n_2+n_3+n_4+n_5+n_6\|}$$

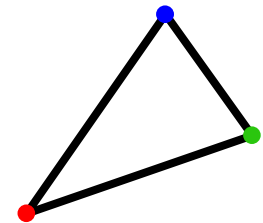
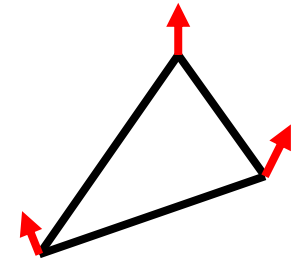
- Use a vertex normal for each vertex
 - For smooth shading, a vertex normal is commonly set to the average of normals of all faces sharing the vertex.

Gouraud Shading



Henri Gouraud
(1944~)

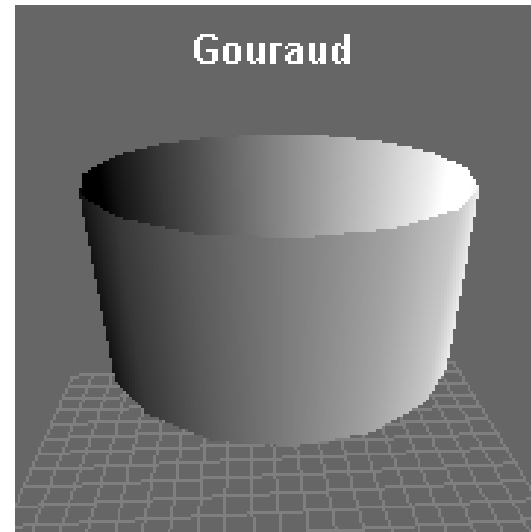
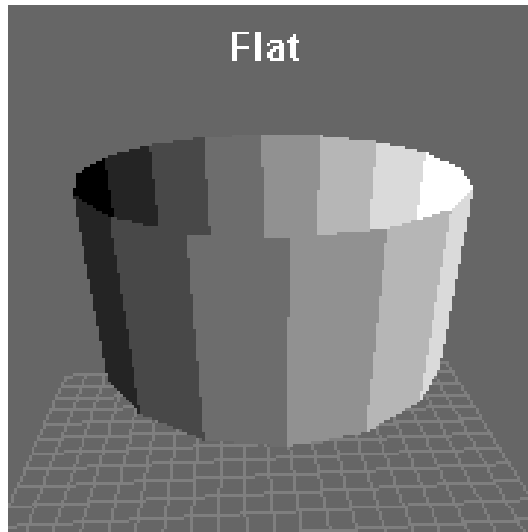
- Use a single vertex normal for each vertex
- Calculate color (by illumination) at each vertex
- Interpolate vertex colors across polygon
 - Barycentric interpolation



See more for barycentric interpolation:

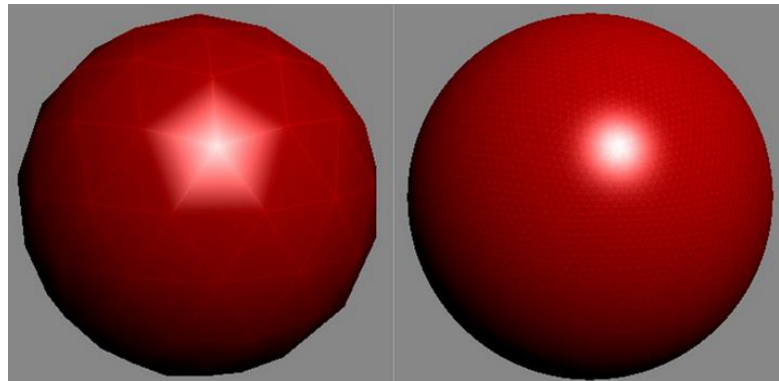
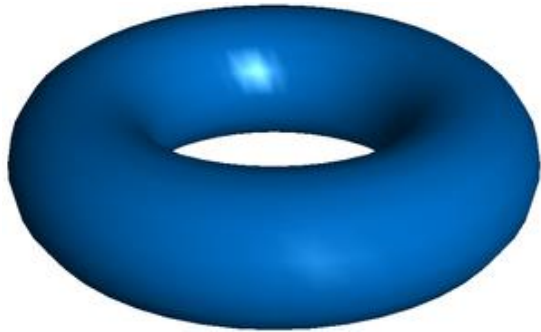
<https://www.scratchapixel.com/lessons/3d-basic-rendering/ray-tracing-rendering-a-triangle/barycentric-coordinates>

Gouraud Shading



Gouraud Shading

- Problem: poor specular highlight
 - Specular highlights may be distorted or averaged away altogether



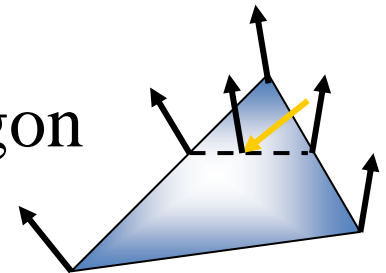
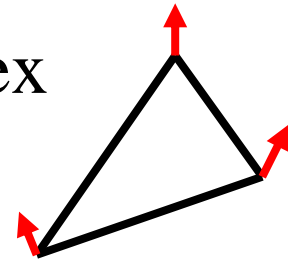
Higher polygon count
reduces this artifact

Phong Shading

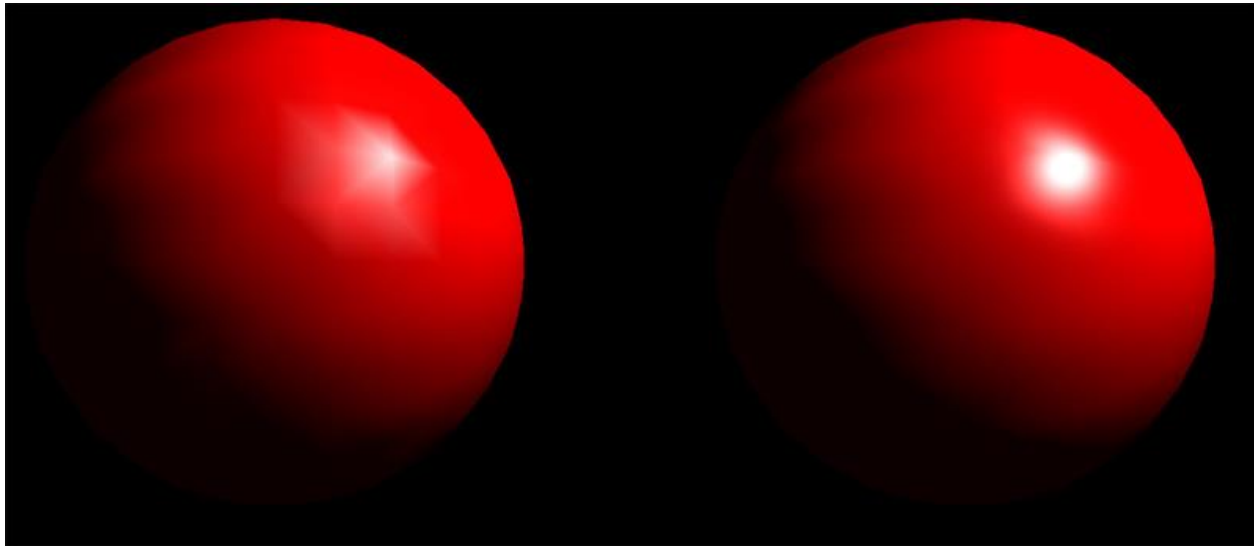


Bùi Tường Phong
(1942 – 1975)

- Use a single vertex normal for each vertex
- Interpolate vertex normals across polygon
- Calculate color (by illumination) at each pixel in polygon using the interpolated normal



Phong Shading



Gouraud shading

Phong shading

Phong Shading

- Captures highlights much better
 - The interpolated normal at each interior pixel is more accurate representation of true surface normal at each point
 - Higher quality, but needs more computation
- Not to be confused with Phong's illumination model (developed by the same person)

[Practice] Online Shading Demos

- Flat & Gouraud shading
 - <http://math.hws.edu/graphicsbook/demos/c4/smooth-vs-flat.html>
- Gouraud & Phong shading
 - <http://www.cs.toronto.edu/~jacobson/phong-demo/>

Next Time

- Lab for this lecture (next Monday):
 - Lab assignment 7

- Next lecture:
 - 8 - Lighting & Shading 2, Hierarchical Modeling

- Acknowledgement: Some materials come from the lecture slides of
 - Prof. Andy van Dam, Brown Univ., <http://cs.brown.edu/courses/csci1230/lectures.shtml>
 - Prof. Jinxiang Chai, Texas A&M Univ., http://faculty.cs.tamu.edu/jchai/csce441_2016spring/lectures.html
 - Prof. Steve Marschner, Cornell Univ., <http://www.cs.cornell.edu/courses/cs4620/2014fa/index.shtml>
 - Prof. JungHyun Han, Korea Univ., <http://media.korea.ac.kr/book/>